

## send-minimal-realizable<sup>11,40</sup>

$$\begin{aligned}
& \forall T:\text{Type}, t:T, l:\text{IdLnk}, ds_1, ds_2:x:\text{Id fp} \rightarrow \text{Type}, P:(\text{State}(ds_1) \rightarrow \mathbb{N} \rightarrow \mathbb{B}), Q:(\text{State}(ds_2) \rightarrow \mathbb{N} \rightarrow \mathbb{B}), \\
& d_1:(\forall s:\text{State}(ds_1). \text{Dec}(\exists n:\mathbb{N}. (\uparrow(\neg_b(P(s,n)))))), \\
& d_2:(\forall s:\text{State}(ds_2). \text{Dec}(\exists n:\mathbb{N}. (\uparrow(\neg_b(Q(s,n)))))), f:(\text{State}(ds_1) \rightarrow \mathbb{N} \rightarrow T). \\
& \text{Normal}(ds_1) \\
& \Rightarrow \text{Normal}(ds_2) \\
& \Rightarrow (\neg(\text{destination}(l) = \text{source}(l) \in \text{Id})) \\
& \Rightarrow \vdash es.\text{@source}(l) \text{ state } ds_1 \ \& \ (\forall e:\text{E}. (\text{kind}(e) = \text{rcv}(l, \text{"tg"}) \in \text{Knd}) \Rightarrow (\text{valtype}(e) \subseteq_r T)) \\
& \quad \& \ \text{@destination}(l) \text{ state } ds_2 \\
& \quad \& \ (\forall e:\text{E}. (\text{kind}(e) = \text{rcv}(\text{lnk-inv}(l), \text{"tg"}) \in \text{Knd}) \Rightarrow (\text{valtype}(e) \subseteq_r \mathbb{Z})) \\
& \quad \& \ (\text{@source}(l) \text{ discrete } ds_1 \\
& \quad \quad \Rightarrow \text{@destination}(l) \text{ discrete } ds_2 \\
& \quad \quad \Rightarrow (\forall k:\mathbb{N}. \text{@source}(l) \text{ stable } s.\uparrow(P(s,k)) ) \\
& \quad \quad \Rightarrow (\forall k:\mathbb{N}. \text{@destination}(l) \text{ stable } s.\uparrow(Q(s,k)) ) \\
& \quad \quad \Rightarrow (\forall k:\mathbb{N}. \\
& \quad \quad \quad \forall e\text{@source}(l). \\
& \quad \quad \quad (\uparrow(P((\text{discrete state after } e),k))) \\
& \quad \quad \quad \Rightarrow \exists e'\text{@destination}(l).(\uparrow(Q((\text{discrete state when } e'),k))) \\
& \quad \quad \quad \quad \vee (\forall n:\mathbb{N}. \uparrow(Q((\text{discrete state after } e'),n)))))) \\
& \quad \Rightarrow (\forall e:\text{E}. \\
& \quad \quad (\text{kind}(e) = \text{rcv}(\text{lnk-inv}(l), \text{"tg"}) \in \text{Knd}) \\
& \quad \quad \Rightarrow (\forall k:\mathbb{N}. (k < \text{val}(e)) \Rightarrow (\uparrow(P((\text{discrete state after } e),k)))))) \\
& \quad \Rightarrow (\forall k:\mathbb{N}, e:\text{E}. \\
& \quad \quad (\text{kind}(e) = \text{rcv}(l, \text{"tg"}) \in \text{Knd}) \\
& \quad \quad \Rightarrow (\text{val}(e) = f((\text{state when sender}(e),k)) \in T) \\
& \quad \quad \Rightarrow (\uparrow(Q((\text{discrete state after } e),k)))) \\
& \quad \Rightarrow \exists e\text{@destination}(l).\text{True} \\
& \quad \Rightarrow (\forall k:\mathbb{N}. \\
& \quad \quad \exists e\text{@destination}(l).(\forall n:\{0..k^-\}. \uparrow(Q((\text{discrete state when } e),n))) \\
& \quad \quad \quad \vee (\forall n:\mathbb{N}. \uparrow(Q((\text{discrete state after } e),n))))))
\end{aligned}$$